PRACTICAL GEOMETRY:

Or, A NEW and EASY

METHOD

OF

TREATING THAT ART.

WHEREBY

The PRACTICE of it is rendered plain and familiar, and the Student is directed in the most easy Manner through the several Parts and Progressions of it.

Translated from the French of Monsieur S. LE CLERC.

The FIFTH EDITION.

Illustrated with Eighty COPPER-PLATES.

Wherein, besides the several Geometrical Figures, are contained many Examples of LANDSKIPS, Pieces of CHITECTURE, PERSPECTIVE, Draughts of GURES, RUINS, &c.

LONDON:

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GEOMETRY

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GENERAL

EDMETRY is a Greek word, and in its native fignification flands for no more than the measuring of land; but now we mean by it the principal part of Mathematicks, which is a science that has continued quantity for its object.

That quantity is called continued quantity, which has all its parts conjoin'd; of this kind are all forts of extension, magnitudes, and dimen-

fions.

And these dimensions consist chiesly either in lines, or surfaces, or angles, or bodies, which last are not to be consider'd in respect of the quality of their matter, but of the extension of their parts.

Geometry is ded into speculative and

practical.

The former is a science that teaches the mind how to form ideas of, and demonstrate the truth of geometrical propositions.

The latter, or practical Geometry, conducts

the hand in working

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Original of Geometry.

CEometry had its original among the Egyptians, who were put under a necessity of inventing some such art to remedy the disorders, that commonly happen'd in their lands, by the overflowing of the Nile, which carried away their land-marks, and effaced the limits of their inheritances.

So that this practice, which in those days confisted only in measuring of land, that every one might have what belonged to him before the

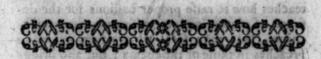
overflow, was call'd Geometry.

d into thecolorive and

But in process of time, the Egyptians applied themselves to more subtle inquiries, and by degrees insensibly there arose from a practice altogether mechanical, a science that now holds the first place among all the others, according to its merit.

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THE Usefulness of Geometry.

GEometry is not only useful, but in several cases necessary. 'Tis owing to this, that Aftronomers are put into a way of making their observations, coming at the knowledge of the extent of the heavens, duration of time, motions of the heavenly bodies, measures of seafons, of years, and of ages.

'Tis by the affiftance of this science that Geographers present to our view at once, the magnitude of the whole earth, the vast extent of the feas, the divisions of Empires, King-

doms, and Provinces.

'Tis from this that the Architects take their just measures for the structure of publick build-

ings, as well as of private houses.

By its help Engineers conduct all their works, take the fituario and plan of places, measure their distances from one another, and carry their measures into places that are only accessible by the eye.

Persons of Quality, whose birth engages them to take the field, are oblig'd to apply themselves to this science. It not only serves as an intro duction

OF GEOMETRY, &c.

duction into the art of Fortification, which teaches how to raise proper bastions for the defence of places, and to raise and manage machines, that may serve to overturn or make breaches in those of the enemy; but also brings them to great skill and dexterity in the art of war, in forming an army into order for battle, in encamping, dividing the ground for quartering the army, taking maps of counties, plans of towns, forts, and castles, measuring all sorts of dimensions, both accessible and inaccessible, and in forming designs; finally to recommend them as much for their skill and address, as for their strength and courage.

All such as profess the Art of Designing, ought to know something of Geometry, seeing that without it they can't make themselves masters of Architecture, nor Perspective, which are two parts absolutely necessary to their art.



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PRINCIPLES

OF

GEOMETRY.

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Principles of Geometry.

C Eometry is built upon three forts of principles, viz. Definitions, Axioms, and Petitions.

Definitions are brief explications of the names

of things, or terms of art.

Axioms are propositions so true and evident, that 'tis impossible to question or contest their truth.

 Petitions are demands so easy and intelligible, that the execution and putting them in practice, require no demonstration.



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DEFINITIONS.

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Definition of a Point.

A Point is that which has no parts.

By this definition you may easily perceive, that a point bas neither length, nor breadth, nor depth; that it is not any thing sensible, but only intellectual; for nothing falls under the notice of our senses, that has nothing of quantity, and nothing is quantity, that has not parts; so that to fay a point is fenfible, would be to fay it has parts, which would contradict this definition. Notwithstanding fince no operation can be perform'd without the intervention of something corporeal, we usually represent a mathematical point by a phylical point, which is an object of fight the smallest and the least sensible that can be, and which has no geometrical magnitude divisible to our fenses, and is made by the prick of a pin, point of a compass, pen or pencil, as the point marked

A central point, or centre, is a point from which a circle, or circumference is described; or rather it is the middle of a figure, as the point

A fecant point, or as some call it, a point of intersection, is a point where two or more lines cross one another, as the point C

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Definition of a Line.

A Line is a length without any breadth.

A line is nothing but the track made by a point passing from one place to another, and would not be perceived, if it were not delineated by a physical point, which by its motion represents a line to us, as

There are as many forts of lines as there are different kinds of motions, which a point, the principle of a line, is capable of; the there are but two which are simple and the principal, viz. a right and curve, and a third which is call a mixt line, because made up of the two former, that are usually consider d in Geometry.

A right line is one that lies equally between its extremities.

Otherwise, tis a line that goes from one point to another without any deviation, as A B

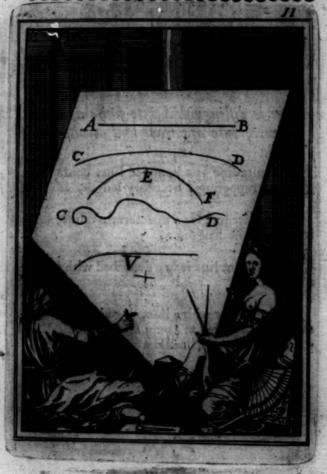
A curve line is that which turns out of its way by one or more deviations, as CD

When such a line as this is described by a pair of compasses, 'tis call'd a circular line, as E

A mixt line is that which is both straight and a curve, as the line

of GEOMETRY.

II





A line is distinguished into finite and infinite, into apparent and occult.

A Finite line is a bounded line, containing or supposing a necessary length, as

An infinite line is an undetermin'd line, having no precise length, as

An apparent line is one described with ink or a pencil, as

An occult, or white line, is only made with the point of a pair of compasses, or mark'd by points, and then 'tis call'd a prick'd line, as C







A line receives also several denominations, according to its different positions and properties.

A Perpendicular is a right line that is let fall or crected upon another, making the angles on each fide equal, as

A Flumb line is that which hangs down without inclining to the right or to the left, and would pass thro' the center of the earth, if it were produced infinitely, as

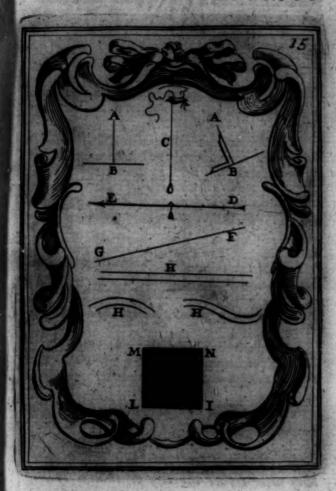
An Horizontal line is a line in equilibrio, equally inclin'd on both fides DE

Parallel lines are fuch as follow one another at an equal distance H

An Oblique line is one that is neither horizontal nor perpendicular F G

A Base is a line upon which the figure rests, as

Sides are the lines that contain a figure, as I N, L M





A Diagonal is a right line croffing a figure, and terminated at its two opposite angles A B

A Diameter is a right line passing through the center of a circle, and terminated at the circumference

A Spiral line is a curve line issuing from a center, and continually going off from it at every turn

A Chord or subtense is a right line that joins the two extremities of an arc

An Arc is any part of a circumference GIH

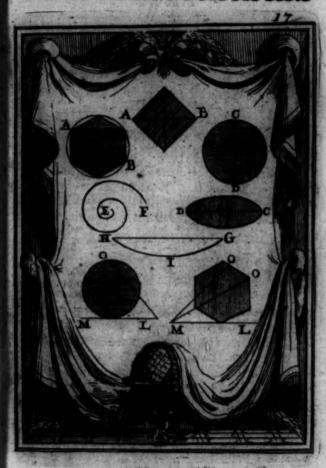
A Tangent is a line that touches a figure without cutting it, nor would it cut or cross the figure, though it were produced, as L M

A Secant is a line that does cross or cut a figure LO, MO

If two lines meet at their extremities, they meet either directly or indirectly; if directly, they make but one line, if indirectly, they form an angle:

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Definition of an Angle.

N Angle is the indirect concourse of two lines in the same point, or rather it is the space contain'd between the indirect concourse of two lines meeting in a point, as

If the concourse be form'd by two right lines, the angle is call'd a Rectilineal, if by two curve lines, a Curvilineal, but if by one right and one curve line, a Mixtilineal angle.

A denotes a rettilineal angle.

B a curvilineal angle.

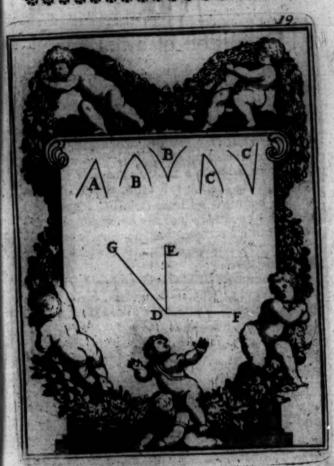
C a mixtilineal or compound argle.

A rectilineal angle receives feveral particular names, according as it has a greater or less aperture, as right, acute, obtuse; thus the terms of rectilineal, curvilineal and mixt, express the quality of the lines, and those of right, acute, obtuse, the quantity of the space contain'd between the faid lines.

An angle is right, when one of the lines is perpendicular to the other

An angle is acute when its aperture is less than that of a right angle EDG

An angle is obtuse when its aperture is greater than that of a right angle FDG The middle letter D denotes the angle.



B 3

THE

Definition of a Surface.

Surface is whatever has length and bread b without depth or thickness.

According to the fentiments of the Geometricians, a Surface is a production of a line, just as a line is the production of a point; thus we are to imagine the line EF moving towards GH to constitute the surface EF GH, which is an extension bounded by lines, and has length and breadth without depth or thickness; this is commonly call'd a furface, but a figure if it be confider'd in regard of its extremities, which are the bounding lines.

If the Surface be elevated or rais'd, 'tis faid to be Convex; but if depressed, sunk in, or hollow, 'tis call'd a Concave; and if even and

flat, a Plane. Thus

B is a Convex Surface.

C a Concave Surface.

A a Plane Surface.

D a Surface that is Convex, Concave and Plane.

This first part relates only to plane Surfaces. The terminus, term or boundary of any thing is its extremity: thus a point is the terminus of a line, a line is the term of a surface, and a surface. is the terminus of a body.

21



Of Surfaces or Figures that are Rectilineal.

Surfaces take their particular names from the number of their fides; thus A TS a Trigon or triangle, a figure with three

fides.

B a Tetragon or square, a figure of four fides.

C a Pentagon, or a figure of five fides.

D an Hexagon, or figure of fix fides. E an Heptagon, or figure of feven fides.

F an Octagon, or figure of eight fides.
G an Enneagon, or figure of nine fides.

H a Decagon, or figure of ten fides.

1 an Hendecagon, or figure of eleven fides. L a Dodecagon, or figure of twelve fides.

All these figures are also call'd by the general name of Polygons.

OF TRIANGLES.

Triangles are distinguished by the quality of their angles, and by the disposition of their sides. Thus

M is a right-angled Triangle, i. e has one right

N an obtuse-angled Triangle, i. e. has one ob-

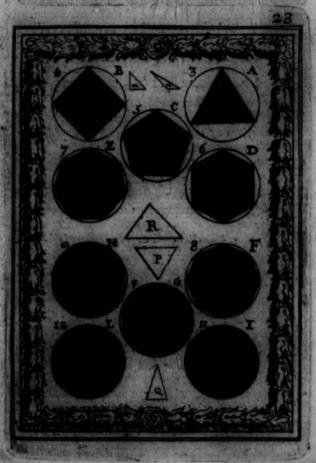
O an acute-angled Triangle, i. e. has all three

P an equilateral Triangle, i.e. has its three fides

Q an isosceles Triangle, i. e. has only two sides

R a Scalene Triangle, i. e. has all its three fides unequal.





Of Quadrilaterals, or figures that have four fides.

A Y S a square or figure that has its four fides

equal and four angles right

B a Rectangle, by some improperly call'd a long square, has all its angles right or equal, but its sides unequal.

C a Rhombus is a Quadrilateral that has its four

fides equal, but not its four and les

D a Rhomboid has the opposite angles and fides equal, without being equiangular or equilateral.

A B C D a Parallelogram is a Quadrilateral whose opposite sides are parallel.

E a Trapezium has only two opposite fides parallel, and the two others equal.

F a Trapezoid has its four fides and angles un-

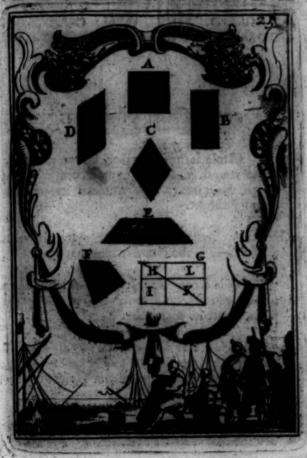
equal.

G if a Diagonal be drawn in a parallelogram, as also two lines parallel to the lader, through the same point of the Diagonal, the parallelogram will be divided into sour parallelograms; and three of them, viz. one of those describes upon the diameter and the two supplements. (i. s. the two parallelograms, which are not described about the diameter) form a signre called a Gnomon; thus the three parallelograms H I L make a Gnomon, as do also the three parallelograms I K L.

All figures baving more than four fides, are call d Polygonals or Multilaterals.

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Curves or Curvilineal figures.

- A Circle is a furface or figure perfectly round, describ'd upon a center, from which the circumference in all its parts is equally distant.
- a b c d. A Circumference is the extremity of a circle, or it is the circular line that bounds it.
- B an Oval is a curvilineal figure describ'd upon feveral centers, and divided into two equal parts by all its diameters.
- C an Ellipse is also a curvilineal figure describ'd upon several centers in the shape of an egg, and has but one diameter that divides it into two equal parts.
- D a Volute or Scroll is a figure or furface bounded by a spiral line.
- E is a Cylindric furface.
- F is an irregular curvilineal figure, compos'd of feveral diffimilar curve lines. 2

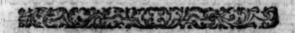
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Proposition of the content.



OF

Compound Figures.

- A Semicircle is a figure contain'd between half the circumference and the diameter.
- B a portion of a Circle is a figure comprehended within any part of a circle and a right line.
- g a large portion of a circle is greater than half the circle.
- f a small portion of a circle is that which is less than half the circle.
- C a Sector is a figure contain'd between two femidiameters and an arc, greater or less than a femicircle.

There is also a large or small Sector.

- D Concentric figures are fuch as have the fame center.
- E Excentric figures are fuch as are describ'd upon different centers.

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OF

Regular and Irregular Figures.

A Regular figure is that which has its op-

B an Irregular figure is fuch an one as is compos'd of angles and fides that are diffimilar.

E E Similar figures are such as have all their sides proportional, though one may be greater, equal or less than another.

F F equal figures are such whose contents are equal, though they may be similar or dissimilar.

C an Equiangular figure has all its angles equal.

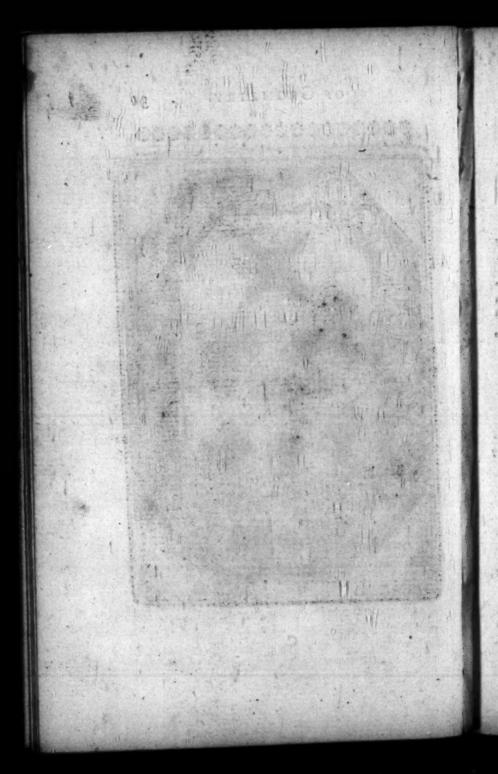
E E one figure is said to be similar or equiangular to another, when all the respective angles of the one, are equal to all the respective angles of the other.

CD an Equilateral figure is one that has all its

fides equal.

G G Similar curvilineal figures are fuch as will admit fimilar Polygons to be inscribed in them, or circumscrib d about them.





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AXIOMS.

Hings equal to the same third, are equal to one another.

The lines A C, A C, which are equal to A B, are also equal to one another.

II.

If to equal things, equal things be added, the whole will be equal.

The lines A C, A C are equal, The lines C D, C D added are equal, The whole A D, A D are also equal.

III.

If from equal things, equal things be taken away, the remainders will be equal.

If from the equal lines AD, AD you take away the equal lines AC, AC the remaining parts CD, CD will be also equal.

IV.

If to unequal things, you add equal things, the whole will be unequal.

If to the unequal lines

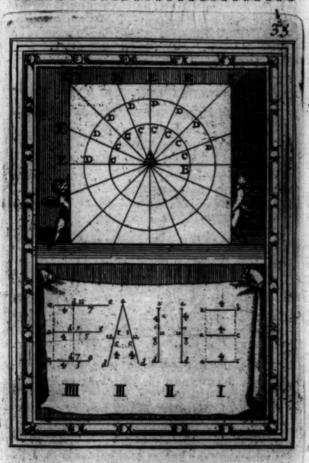
you add the equal lines

the whole

will be unequal.

D F, D E
A D, A D
A E, A E





V.

If from unequal things, equal things be taken, the remainders will be unequal.

If from the unequal lines, AE, AE you take away the equals, AD, AD the remainders, DE, DE will be unequal.

VI.

Things double the same third, are also equal to one another.

The right lines DD, DD that are double the line AD are equal among themselves,

VII.

Things, that are balves of the same, or equal things, are also equal.

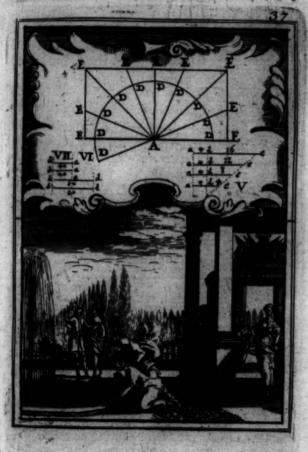
The lines A D, A D which are the halves of the lines D D, D D are equal to one another.

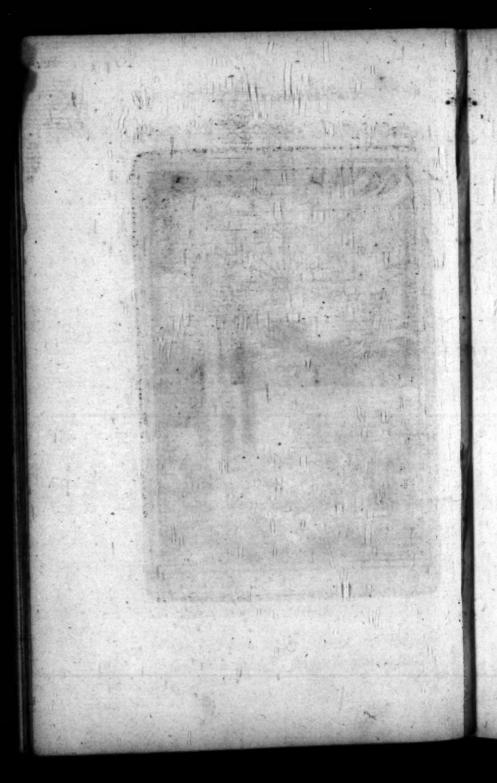
What bas been said of lines, may also be said of numbers, surfaces and bodies.

OF GEOMETRY.

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PETITIONS.

Editional to regularity



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Petitions or Demands.

PETITION I.

D	Raw a	right	line	from	the p	point	A
L	Raw a to the	point		T	17	17	B

OPERATION.

Apply a ruler to the points	A & B
Draw the line demanded	A B
by carrying the pencil along	the ruler,
and close to it from the point	A
to the point	B

PETITION II.

Produce infinitely the line	C	D
on the fide of the extremity		D

Join the ruler to the line	CD
Continue infinitely that line	CD
on the fide of the extremity	D
by carrying the pen along ruler towards 2	close to the

OF GEOMETRY.

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PETITION III.

Describe a circle upon the point	A
and at the distance	AB

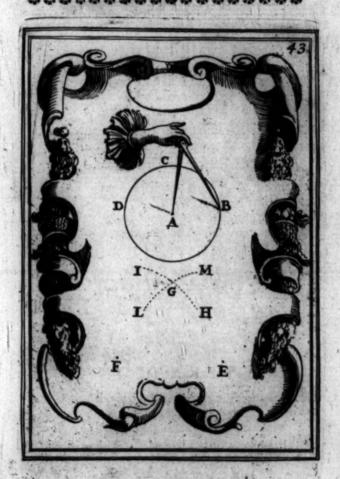
Set	one of the points of the compass	
330	upon the given point	A
	en the other to the given point	B
Tu	rn the compasses about upon the point	A
	and trailing the point	B
170	draw the circle demanded BC	D

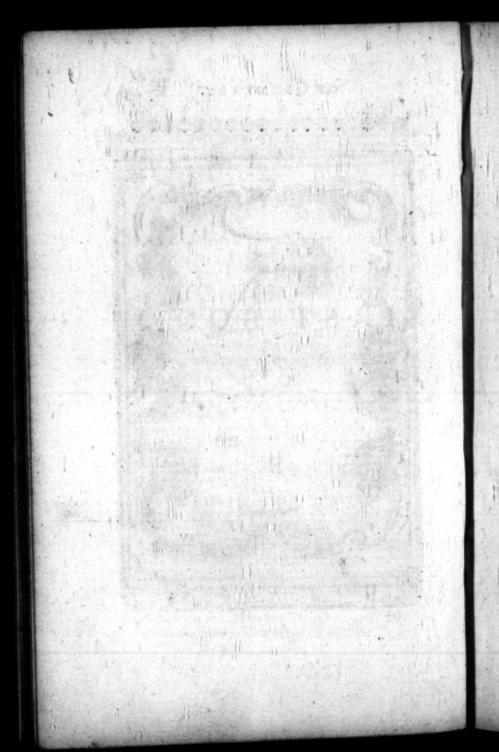
PETITION

On the points	2414	E&	F
make an intersection or	section.	The Royal	

Open the compasses at discretion, but so t	hat
the distance of the two points of the co	m-
passes may be greater than half the dista	nce
of the points proposed E	e F
With this distance of the compasses	STATE OF
	M
and the interfection requir'd will be	HIG
and the microcaon redain a Mili ps	J

of Geometry. 43





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Description of Lines.

BOOK the FIRST.

PROPOSITION I:

To erect a perpendicular upon the middle of a right line.

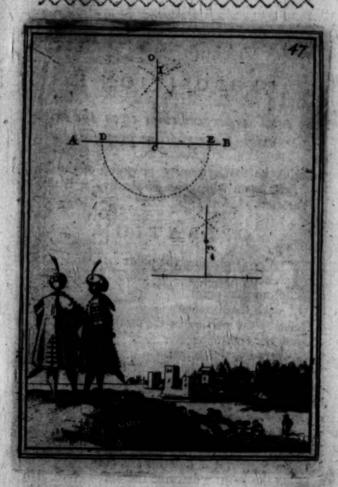
POSITION.

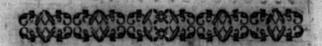
Let C be the point proposed in the middle of the line A B, upon which the perpendicular is to be erected.

OPERATION.

U Pon the given point describe at pleasure the semicircle	DE
upon the points	D&E
make the fection	I
from the point	C
draw the line demanded	CO
thro' the fection	1

This line C O will be perpendicular to the line given A B, and erected upon the point proposed C.





PROPOSITION II.

To erect a perpendicular upon the extremity of a right line proposed.

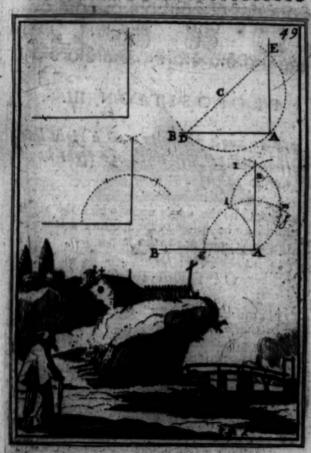
Let A be the extremity proposed of the line A B, upon which the perpendicular is to be erected.

OPERATION.

Ake at pleasure the point	C
above the line	AB
from that point	C
with the distance	CA
Describe the portion of the circle	EAD
Draw the right line	DICE
through the points	D&C
Draw the line demanded	AE
it will be perpendicular to	AR
and at the extremity proposed	A

Another way.

Upon the point A describe the arc	ghm
Upon the point g describe the arc	Ah
Upon the point h describe the arc	Amn
Upon the point m describe the art	hn
Draw the line requir'd	AR





PROPOSITION III.

Upon an angle given to erest a right line that inclines neither to the right hand nor to the left.

Let B A C be the angle upon which the right line is to be raised, that inclines neither to the right hand nor to the left.

OPERATION.

T TPon the angle given	A
U Pon the angle given describe at pleasure the arc	BC
upon the extremities	B&C
make the fection	D
fr m the point of the angle given	A
draw the line requir'd	AD
through the fection	D

This right line

A D

shall be erected upon the angle

without inclining either to the right or left.







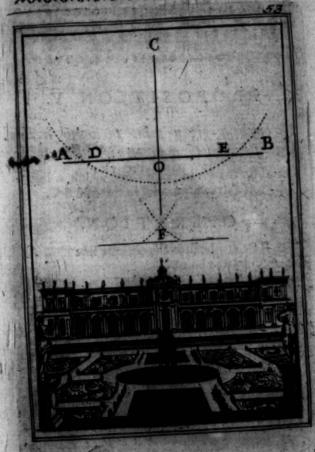
PROPOSITION IV.

To let fall a perpendicular upon a given line, from a point without the line.

Let C be the point from which a line is to be let fall perpendicular to A B.

T TPon the given point	C
describe at pleasure the arc	DE
cutting the line	AB
in the points	D&E
upon those points	D&E
As centers make the section	F
draw the line	CF
and the line	CO
will be the line requir'd	AND DESCRIPTION OF THE PARTY OF







PROPOSITION V.

Through a given point to draw a line parallel to a given right line.

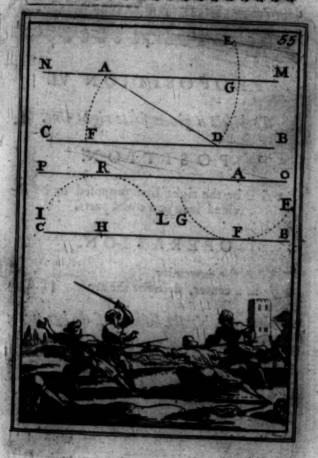
Let A be the given point thro' which a line is to be drawn parallel to the line B C.

OPERATION.

Raw at pleasure	the oblique line	AD
Describe the arc		DE
upon the point		D
Describe the arc		AF
make the arc		DG
Draw the line require	d	MN
thro' the points	Held Street	A&G

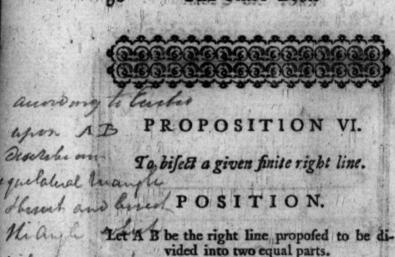
Otherwife.

Upon the center A describe the arc	EFG
touching the line	BC
without altering the legs of the comp	affes.
Upon the point H describe the arc	LRI
The point H is taken at pleasure in the	line B C
Draw the demanded line	OP
thro' the point	A
and touching the arc	LRI



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OPERATION.

UPon the extremity
as a center, describe the arc CD

Without altering the distance of the legs of the compasses.

Upon the other extremity

as a center, describe the arc

E F

These arcs are to be made so as to intersect each other.

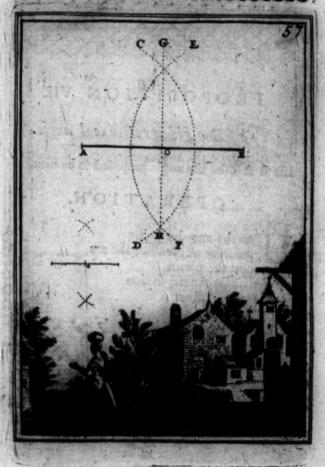
Draw the right line

through the interfections

A B then will be bifected at the point

G H

G & H





PROPOSITION VII.

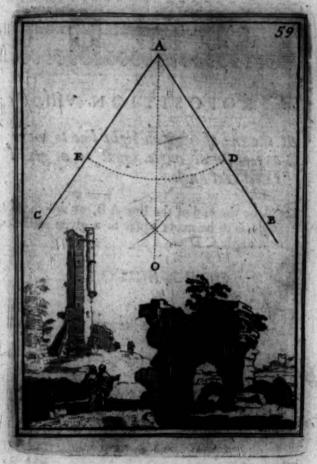
To bifett a given retilineal angle.

Let B A C be the angle proposed to be bisected.

T TPon the angular point	A
describe at pleasure the arc	DE
upon the points	D&E
As centers make the fection	0
draw the line	AO
This line	AO
will divide the given angle	BAC
into two equal parts.	16



of practical Geometry. 59



Hologogy at build say



PROPOSITION VIII.

At the end of a given right line to make a restilineal angle equal to a given restilineal angle.

Let A be the end of the line AB, at which an angle is to be made equal to a given rectilineal angle CDG.

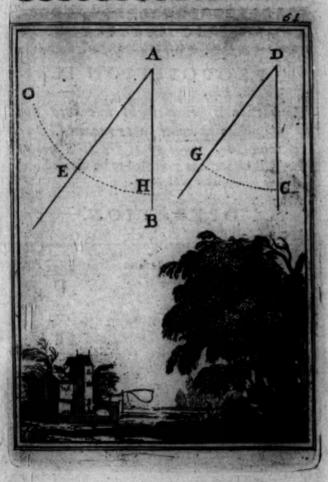
OPERATION.

T 7Pon the angular point	D
U Pon the angular point describe at pleasure the arc	CG

Without altering the opening of the compasses.

Upon the extremity	A
describe the arc	HO
Make the arc	HE
equal to the arc	CG
draw the line	AE
The angle	BAE
will be equal to the angle	CDG
which was the thing proposed.	0 1

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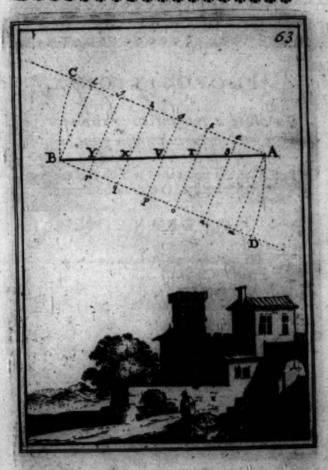
PROPOSITION IX.

To divide a given right line into any number of equal parts requir'd.

Let A B be the line proposed to be divided into fix equal parts.

THE RESERVE OF THE PARTY OF THE	It set the set it.
Rom the point draw at pleasure the line	A
draw at pleasure the line	AC
thro' the extremity	В
Draw the line	, BD
parallel to the line	AC
from the points	A & B
	AC, BD
Carry any fix equal parts, viz.	efghlL
along the line	AC
R q p o n m along the line	BD
draw the lines en, fo, gp	, hq, IR
Then the line	AB
will be divided into fix equal p	arts at the
	V, X, Y
	CONTRACTOR OF THE PARTY OF THE

of practical Geometry. 63





PROPOSITION X.

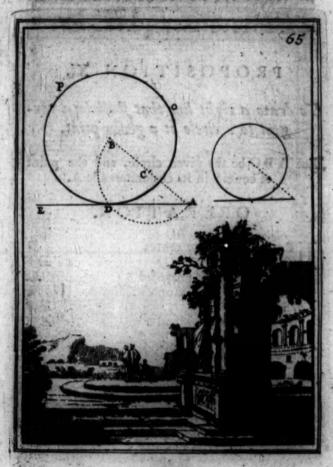
To draw a tangent to a circle proposed through a given point.

Let A be the point thro' which the tangent to the circle D O P is to be drawn.

Rom the center of the circle	B
draw the fecant	BA
divide the line	BA
into two equal parts in	C
upon the point	C
	CA
	DB
cutting the circle in	D
from the given point	A
Draw the right line	AB
thro' the point	D
This right line	AB
will be the tangent requir'd.	

of Practical Geometry. 63

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PROPOSITION XI.

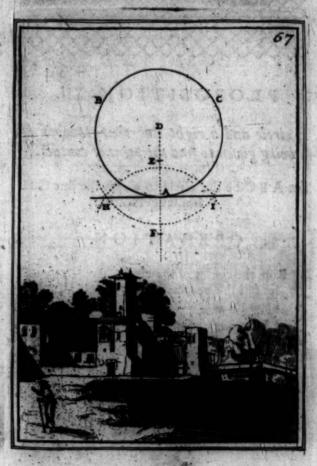
To draw a right line that shall be a tangent to a circle at a given point.

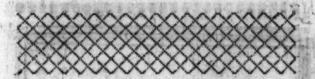
Let ABC be the given circle, and the point of contact in its circumference A.

TRom the point or center	D
draw the line	DF
thro' the point proposed	A.
Thro' the point proposed	A
and to the line	DF
draw the perpendicular	AH
continued towards	1
This tangent	HI
will touch the circle at the point	A
which was the thing required.	









PROPOSITION XII.

A circle and a right line that touches it being given to find the point of contact.

Let A B C be the circle to which the line G H is a tangent.

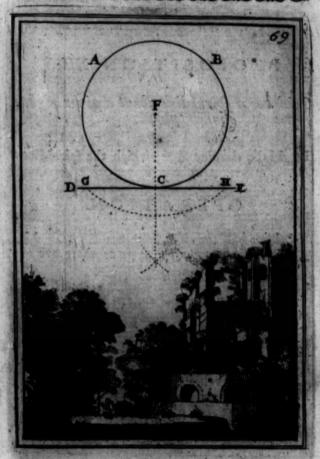
OPERATION.

Pag. 8. Rom the center of the circle
let fall the perpendicular
upon the tangent

The fection
will be the point of contact fought.



of practical Geometry: 69





PROPOSITION XIII.

To draw a spiral line about a given right line.

Let I L be the line about which the spiral line is to be described.

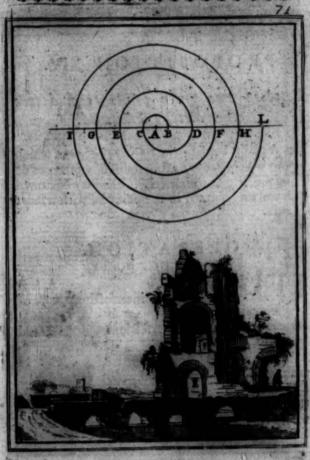
OPERATION.

Pag. 18. Divide half the right line IL. into as many equal parts as there are to be revolutions.

EXAMPLE.

To make one of four revolutions.

Pag. 11. Divide the half
into four equal parts
Divide also
into two equal parts in
upon the point
Describe the semicircles BC, DE, FG, HI
upon the point
Describe the semicircles CD, EF, GH, IL
and you will have the spiral line sought.



PROPOSITION XIV.

Between two given points to find two other directly interposed.

Let A and B be the points given, between which two others are to be found directly interpos'd, by the help of which a right line may be drawn from the point A to the point B, with a short rule.

OPERATION.

Pon the points

as centers, make the intersections C & D

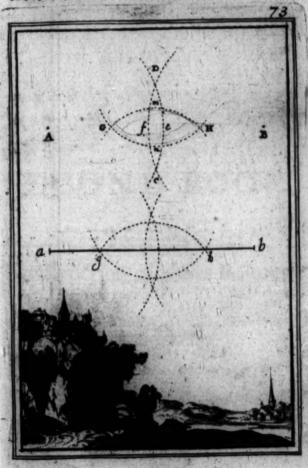
upon the points

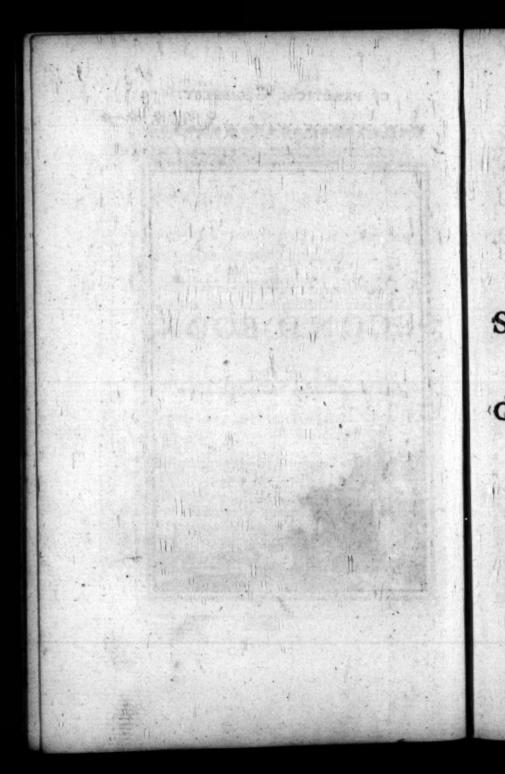
As centers make the intersections

G & H

These points G&H are the points requir'd, by the affistance of which a right line may be drawn from the point A to the point B, which could not be done at once with a rule less than the length between A&B.







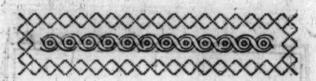
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SECOND BOOK,

OF THE

Construction of plane Figures.



BOOK the SECOND.

PROPOSITION L

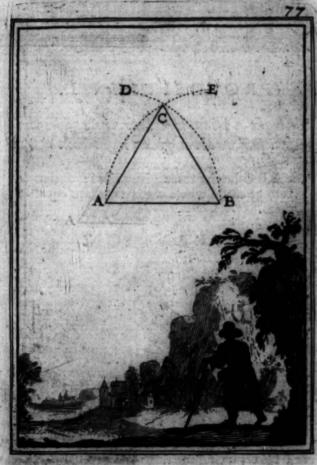
To make an equilateral triangle upon a given line.

Let A B be the given line upon which the equilateral triangle is to be constructed.

OPERATION.

T TPon the extreme point	. A
UPon the extreme point with the radius	AB
Describe the arc	B D
upon the extremity	В
with radius	BA
Describe the arc	AE
from the interfection	C
Draw the lines	CA, CB

A B C will be the equilateral triangle required.





PROPOSITION II.

To make a triangle whose three sides are equal to three given right lines.

Let ABC be the three given lines; a triangle is to be made whose three sides are equal to them.

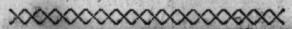
OPERATION.

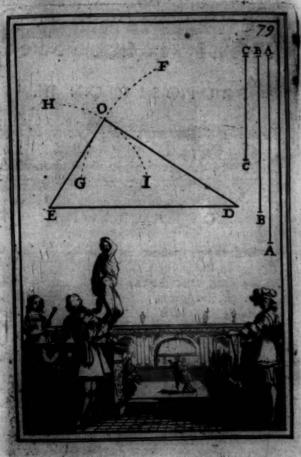
DE
AA
D
BB
GF
E
CC
HI
. 0
DE, OD

The triangle

will be composed of three sides equal to the three lines given

A A, B B, C C.







PROPOSITION III.

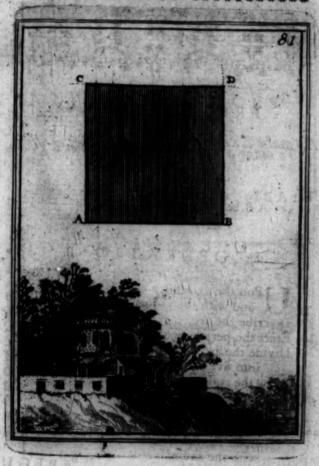
To make a square upon a given right line.

Let A B be the given right line, upon which the square is to be made.

OPERATION.

Pag. 50. TR	ect the perpendic	ular	AC
	upon the point	6.19	A
	center, describe t	he arc	BC
1	apon the points		B& C
	with the radius		AB
Make	the fection	(Alberta September 1997)	D
f	rom the point		D
	the lines	The Table	DC, DB

A B C D will be the square requir'd to be constructed upon the given right line A B.





PROPOSITION IV.

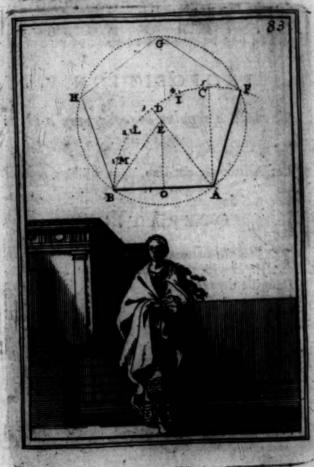
To make a regular pentagon upon a given right line.

Let A B be the given line, upon which the pentagon is to be constructed.

OPERATION.

	T 7 Pon the extremity	A
	U Pon the extremity and with the radius	AB
	Describe the arc	BDF.
Page 50.		AC
	Divide the arc	BC
L. Carlo	into five equal parts	· IDLM
	Draw the right line	AD
Page 58.	Divide the base	AB
	into two equal parts in	D
Page 46.	Erect the perpendicular	OE.
	upon the interfection	EA
1	with the radius	
	Describe the circle	ABFGH
	Carry round five times, the line	AB
	in the circumference of the regular equiangular equilater	
	will be compleated.	

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PROPOSITION V.

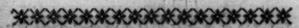
To make a regular bexagon upon a given right line.

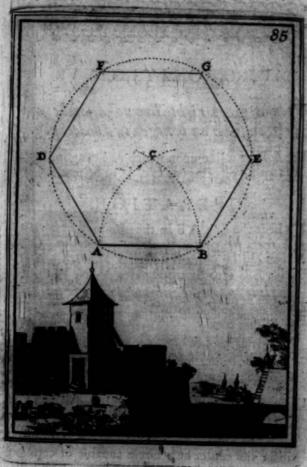
Let A B be a right line, upon which a regular hexagon is to be made.

OPERATION.

U Pon the extremities
and with the radius
Describe the arcs
upon the section
Describe the circle
Carry fix times the line given
in the circumference, and you will have a regular hexagon
upon the given line
A B







Pag. 58. Pag. 46.



PROPOSITION VI.

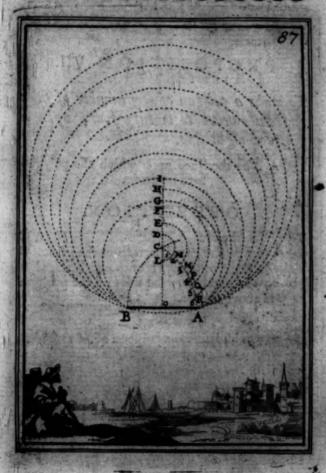
Upon a given right line to describe any polygon from an hexagon to a dodecagon.

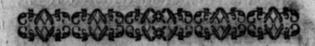
Let A B be a line upon which an hexagon, heptagon, or octagon, &c. is to be made.

OPERATION.

	65686 1 .88
Rifect the line A B in the point	0
Derect the perpendicular	OI
upon the point B describe the arc	AC
Divide A C into fix equal parts M, N, I	
This is to be done, if an heptagon is to be	AND DESCRIPTION OF THE PERSON NAMED IN COLUMN 1
Upon the point C with the interval	E 2 1
of one part	CM
describe the arc	MD
D will be the center for describing a circl	e capa-
ble of containing feven times the line	
For an octagon.	
Upon the center C, with the interval	
of two parts	CN
Describe the arc	NE
E will be the center of a circle capable	RES REGULATION
	AB
taining eight times the given line	
For an heptagon.	
Take three parts	CP
and so for the rest, adding one part.	

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PROPOSITION VII.

To make a polygon of any number of sides from twelve to twenty four, upon a given right line.

Let A B be the line, upon which the polygon is to be made.

OPERATION.

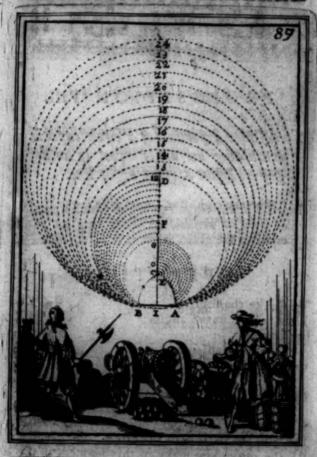
Divide the arc
into twelve equal parts from the point C
Take as many of the parts of CA
as the number of the fides of the polygon
is above twelve.

EXAMPLE.

If you would describe a polygon of fifteen	ides.
Upon the point	C
with the radius of three of these parts	CE
describe the arc	EO
AC of twelve, CO of three together	make
fifteen.	
Upon the point O with the radius	OB
describe the arc	BF
Upon the point F with the radius	FA
describe a circumference, and it will	con-
tain the line given	AB
twelve times.	

and so also for any other polygon.

of practical Geometry. 89





PROPOSITION VIII.

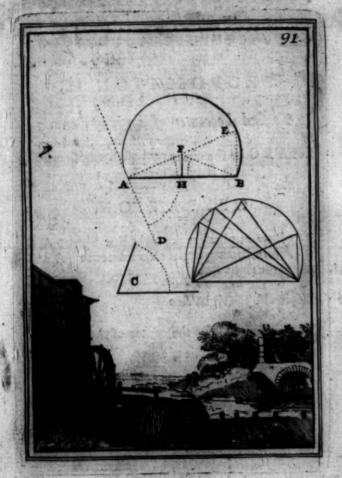
To describe a portion of a circle capable of containing an angle equal to an angle given, upon a given right line.

Let AB be the right line, upon which a portion of a circle capable of containing an angle equal to the given angle is to be described C

OPERATION.

Page 62.	Make the angle BAD equal to the angle
Page 50.	Erect upon AD
	the perpendicular AE
Page 58.	Bifect the line AB
	in the point
Page 46.	Erect the perpendicular HF
	upon the fection F
	with the radius FA
	Describe the portion of the circle AEB
	All the angles you make in this fegment of the
	circle, and upon the given line A B
	will be equal to the angle

of practical Geometry. 91



PROPOSITION IX,

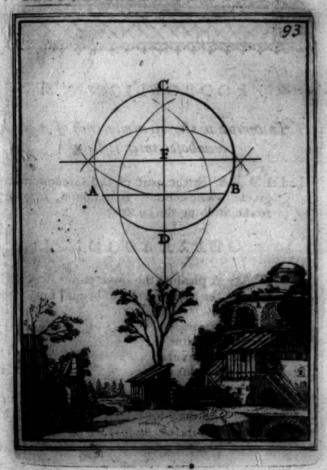
To find the center of a given circle.

Let A B C be the circle proposed, whose center is to be found.

OPERATION.

Raw at pleasure the right line AB terminating in the circumference ABC Bifect the right line Page 58. AB by the line DC Page 58. Bifect also the right line CD in the point F The point F will be the center of the circle requir'd







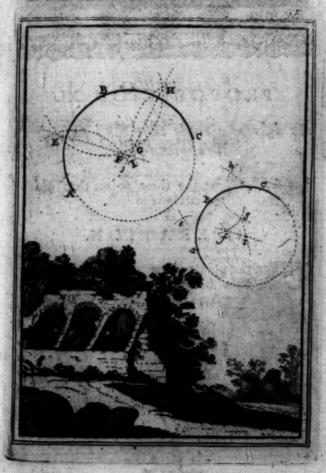
PROPOSITION X.

To compleat the circumference of a circle whose center is lost.

Let A B C be the part of the circumference given, whose center is to be found, in order to the finishing the circle.

OPERATION.

Ake at pleasure the three points ABC in the circumference begun upon the points A & B Make the fections E & F Draw the right line upon the points B&C Make the fections G-& H draw the right line GHupon the interfection and center and with the interval compleat the circumference begun.





PROPOSITION XI.

To describe a circle that shall passithro three given points.

Let A, B, C, be the three points thro' which the circle is to pass.

OPERATION.

U Pon the points given

describe three circles DEH, DEF, FGL
with the same radius, and intersecting at
the points

D & E, F & G

Draw the right lines
till they meet in
upon the point
with the radius

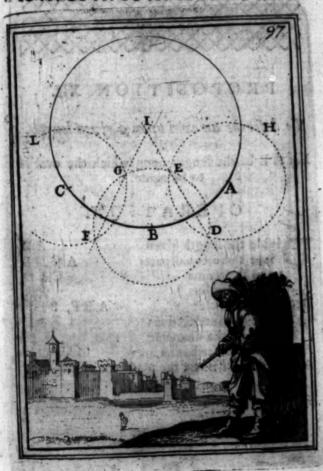
Describe the circle required.

This operation is similar to the preceding.



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PROPOSITION XII.

To describe an oval upon a given length.

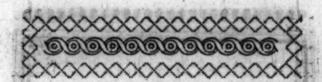
Let A B be the length upon which the oval is to be made.

OPERATION.

Pag. 64. Divide the length given into three equal parts ACDB C&D upon the points with the radius Describe the circles AEF, BEF upon the interfections and with the diameter As a radius, describe the arcs AIHBPO will be the oval requir'd.







PROPOSITION XIII.

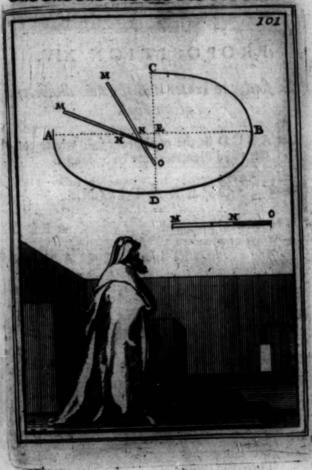
To describe an oval upon two given diameters.

Let A B, C D be the diameters upon which the oval is to be constructed.

OPERATION.

A Ake the ruler	MO
M Ake the ruler equal to the greater femidiameter	AE
upon which mark the length	MN.
equal to the leffer femidiameter	CE
This ruler being thus dispos'd.	
Place it after such a manner upon the dias	neters
	CD
that the point	N
fliding along the line	AB
the extremity	0
may always be in the line	CD
carrying along thus the rule	MO
Describe the oval with the extremity	M

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PROPOSITION XIV.

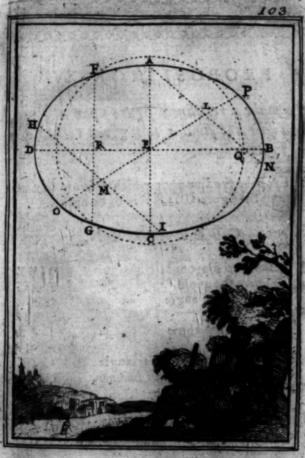
To find the center and the two diameters of an oval.

Let A B C D be the oval proposed, whose cen-

OPERATION.

	N the oval proposed	ABCD
Page c6.	draw at pleasure	
AK	the two parallel lines	AN, HI
Page 56.	Bifect the lines	AN, HI
	in the points	L&M
	Draw the line	PLMO
Page 58.	Biset it in	E
	and the point E will be the	
	upon the point	E
	Describe at pleasure the circle	FGQ
	cutting the oval in	F&G
	thro' the interfections	F&G
	Draw the right line	FG
	Bifect it in	R
JOA	Draw the greatest diameter	BD
		ER
	Thro' the points	
		ARC
Page 50.	Draw the least diameter	AEC
	parallel to the line	FG
	and what was proposed will	be enected.







PROPOSITION XV.

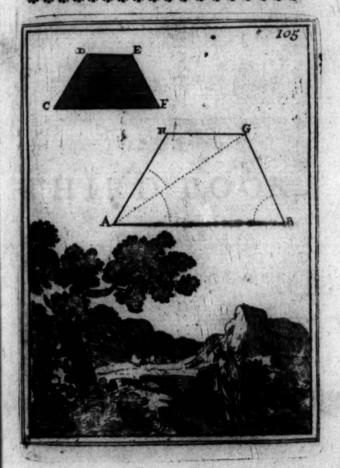
To make a retilineal figure upon a given right line similar to a given retilineal figure.

Let A B be the line upon which a figure similar to the figure C D E F is to be drawn.

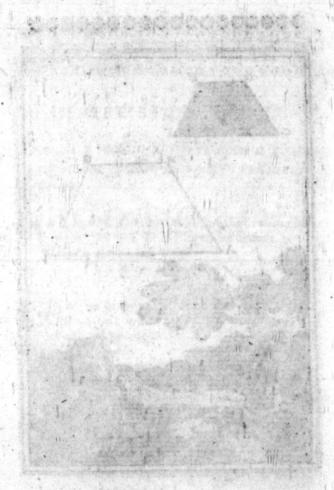
OPERATION.

	Raw the diagonal	CE
Page .62	Paw the diagonal make the angle	ABG
	equal to the angle	CFE
Page 62.	Make the angle	BAG
	equal to the angle	FCE
	the triangle	ABG
	will be fimilar to the triangle	CFE
	After the same manner,	
Page 62.	Make the triangle	AGH
	fimilar to the triangle	CED
		ABGH
	will be fimilar to the whole figure	CDEF

of Practical Geometry. 105



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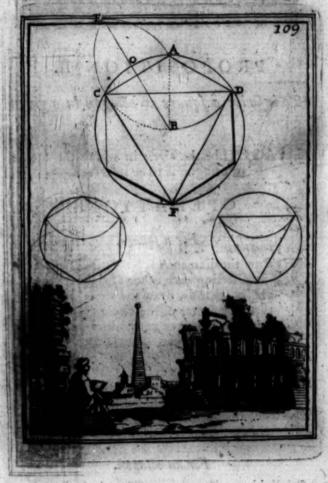
PROPOSITION I.

To inscribe in a given circle, an equilateral triangle, bexagon or dodecagon.

Let A C D be the circle in which an equilateral triangle, &c. is to be inscribed.

	For an equilateral triangle.
	T TPon a point as
	U Pon a point as with the interval of the femidiameter A B.
	Describe an arc CBD
	Draw the right line . DC
	Carry that distance CD
	from the point C
and the	to the point
	Draw the lines FC, FD
	The triangle requir'd will be CDF
	For an hexagon.
	Carry round fix times the femidiameter . AB
	in the given circumference.
	For a dodecagon.
Page 58.	Bifect the arc of the hexagon AC
	in the point O
	the fide of the dodecagon will be AO

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PROPOSITION II.

To inscribe a square or octagon in a given circle.

Let ABCD be the circle in which the square or octagon is to be inscribed.

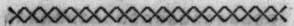
OPERATION.

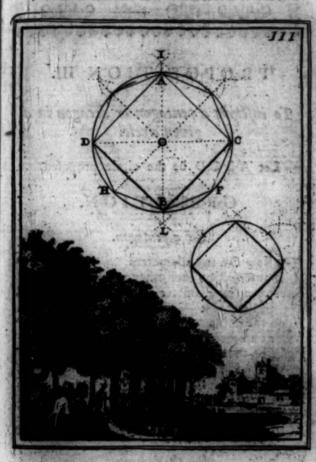
For a Square.

Raw the diameters	AB, CD
DRaw the diameters interfecting each other at right	
angles, that is, than the right	ine CD
thro' the center of the circle	0
upon the points or extremities	C&D
Make the interfections	L& L
Draw the right line	11
paffing thro' the center	0
These lines or diameters	AB, CD
will interfect at right angles.	*
Draw the lines AC, AD, BC, BD,	& ACBD
will be the square requir'd.	

For an octagon.

Subdivide each quarter of the circle into two Page 38. equal parts, and you will have an octagon.





PROPOSITION III.

To inscribe a pentagon or decagon in a given circle.

Let ABCD be the circle proposed.

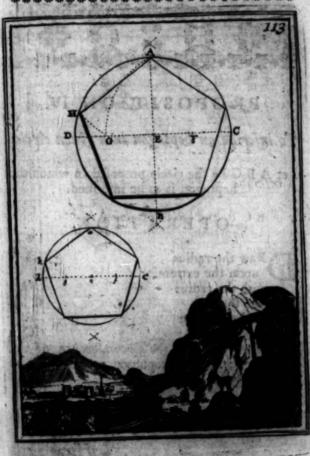
OPERATION.

For a pentagon.

	Raw the two diameters intersecting each other at right ar Bisect the semidiameter	AB, CD
Page 48.	intersecting each other at right ar	igles in E
		CE
	in the point	F.
	Upon the point	F
	as a center, with the radius	FA
	Describe the arc	AG
	upon the point	A
	with the radius	AG
	Describe the arc	GH.
	The right line	AH
1	will divide the circle into five eq	nal parts.

For the decagon.

Page 53. Subdivide each part of the circle into two equal parts.





PROPOSITION IV.

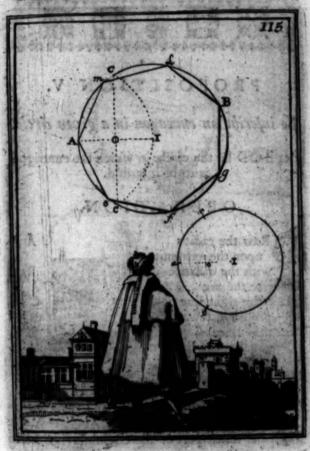
To inscribe an beptagon in a given circle.

Let A B C be the circle proposed in which the heptagon is to be inscribed.

Raw the radius	IA
D upon the extremity	A
with the radius	AI
Describe the arc	CIC
Draw the right line	CC
Carry the half	CO
feven times in the circumference	of the
circle, and the heptagon requir'd	will be
inscribed.	







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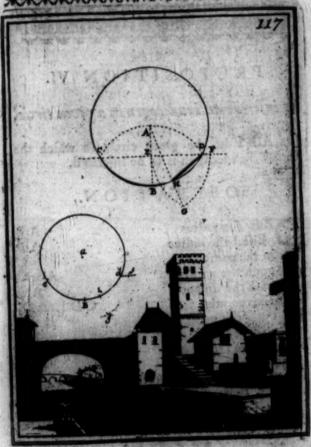


PROPOSITION V.

To inscribe an enneagon in a given circle,

Let B C D be the circle in which the enneagon is to be inscrib'd.

DRaw the radius upon the extremity	AB
upon the extremity	В
with the distance	BA
Describe the arc	CAD
Draw the right line	CD
produced towards	P
Make the line	EF
equal to the line	AB
upon the point	E
Desgribe the arc	FG
upon the point	F
Describe the arc	EG
Draw the line	AG
Then the ninth part of the circum	ference will
be	DH





PROPOSITION VI.

To inscribe an bendecagon in a given circle.

Let A E F be the given circle in which the hendecagon is to be inscrib'd.

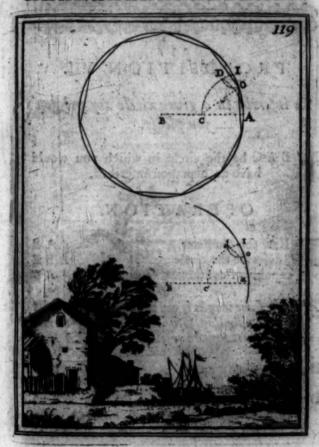
OPERATION.

Pag. 58.

DRaw the radius
Bifect the radius
In the point
Upon the points
With the diffance
Describe the arcs
Upon the point
With the distance
Describe the arc
Upon the point
With the distance
Describe the arc
Upon the point
With the distance
Upon the point
Upon th



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PROPOSITION VII.

To inscribe in a given circle any polygon you please.

Let B A C be the circle in which you would have an heptagon inscribed.

OPERATION.

Pag. 84.

86. 88. 90.

Raw the diameter

describe the circle

capable of containing seven times

A B F

A B

After the same way as if you would make upon AB
a polygon similar to that which is to be inscribed in the given circle
ABG

Pag. 56. Draw the diameter

parallel to the diameter

D E

A B

Draw the right lines

D A G, E B H

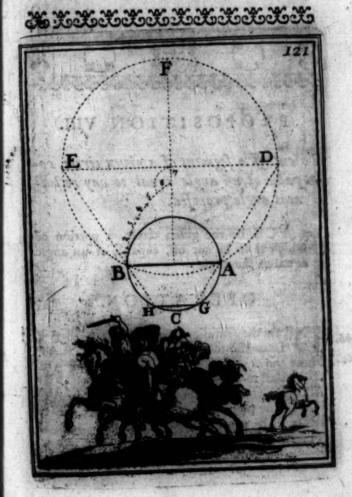
thro' the extremities

D A, E B

G H, will divide the circle given

into feven equal parts.

After the fame manner act in other polygons.





PROPOSITION VIII.

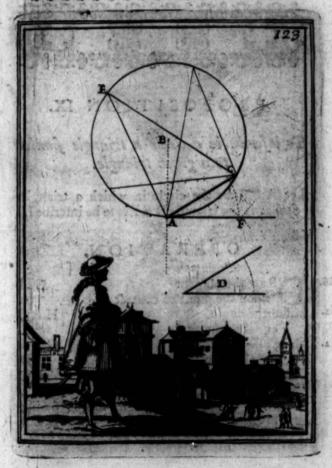
To cut off a segment of a given circle, capable of an angle equal to any restilineal angle proposed.

Let ACE be the given circle, a portion of which is to be cut off, capable of an angle equal to the angle

OPERATION.

Raw the femidiameter Page 66. Draw the tangent AF Page 62. Make the angle equal to the given angle All the angles made upon in the fegment will be equal to the given angle Therefore the portion is the fegment requir'd.

@@@@@@@@@@@@**@@**@**@**



124 THE THIRD BOOK



PROPOSITION IX.

To inscribe in a circle a triangle similar to a given triangle.

Let ABC be the circle in which a triangle fimilar to the triangle DEF is to be inscribed.

OPERATION.

Page 66.	Raw the tangent GH	è.
	upon the point of contact A	į
Page 62.	Make the angle HAC	-
	equal to the angle	
Page 62.	Make also the angle GAB	į.
	equal to the angle	P.
	Draw the line BC	
	A B C will be the triangle requir'd to be fimilar	けっては

CONNES

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PROPOSITION X.

To inscribe a circle in a given triangle:

Let ABC be the triangle in which the circle is to be inscribed.

Page 60-	Difect the angles	B&C
	D by the right lines	BD&CD
	from the intersection	D
Page 54.	Let fall the perpendicular	DF
	Upon the center	D
	with the distance	DF
NECES TO SE	Describe the circle requir'd	BFG







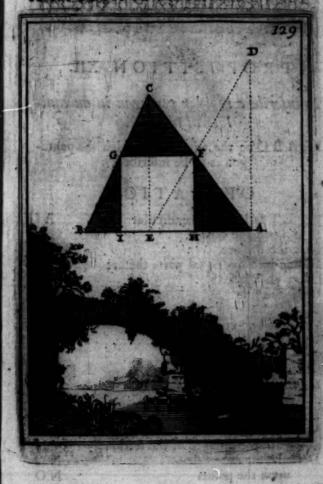
PROPOSITION XI.

To inscribe a square in a given triangle.

Let A B C be the triangle in which the square requir'd is to be inscribed.

Page 50. Rect the perpendicular	AD
upon the extremity of th	e base A B
Make this perpendicular	AD-
equal to the base	AB
from the angle	C
Page 56. Draw the line	CE
parallel to the line	AD
Draw the oblique line	DB
thro' the fection	F
Page 56. Draw the line	FG
parallel to the base	AB
Page 56. Draw the lines	FH, GI
parallel to the line	CE
And the fquare requir'd will b	e FGHI

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PROPOSITION XII.

To inscribe a regular pentagon in an equi-

Let A B C be the triangle in which the pentagon is to be inscribed.

Page 54. LET fall the perpendicular AI upon the center BIM Describe the arc BIM Divide into five equal parts the arc BI Carry on the fixth IM Draw the line AM	
Describe the arc Divide into five equal parts the arc Carry on the fixth B I M B I B I B I B I B I B I B I B I B I B I	Page 54.
Describe the arc Divide into five equal parts the arc Carry on the fixth B I M B I B I B I B I B I B I B I B I B I B I	
Carry on the fixth	
Carry on the fixth	
Diam che illie	
Page cg. Divide AM	
	Page 58.
into two equal parts in L	
Upon the point	
describe the arc LD	
Draw the right line L D to H	
Make the part	
equal to the part BH	
Draw the right lines DG, MC	
upon the center D	
with the distance of the section N	
Describe the arc NO	
upon the points NO	
Describe the arcs DQ, DP	
Draw the lines OP, PQ, NQ	
And the pentagon demanded shall be DOPQN	

A-----





PROPOSITION XIII.

To inscribe an equilateral triangle in a square.

Let A B C D be the fquare in which the equilateral triangle is to be inscribed.

T Raw the diagonals	AC, BD
1 upon the center	E
and with the distance	EA
Describe the circle	ABCD
upon the point	C
with the distance	CE
Describe the arc	GEF
Draw the right lines	AF, AG
Draw the right line	HI
The equilateral triangle requir'd is	AHL



Page 98.

PROPOSITION XIV.

To inscribe an equilateral triangle in a pentagon.

Let ABCDE be the pentagon in which an equilateral triangle is to be inscribed.

	TO A SUPERIOR
Ircumscribe the circle A	BCDE
upon the point.	A
and with the distance of the radius	AF
Describe the arc	FL
Cut that are	FL
into two equal parts in	N
Draw the line	FNI
upon the point	-, A
with the distance	AI
Describe the arc	HOI
draw the lines A	HHI
The triangle demanded will be	AHI
	AND DESCRIPTION OF THE PARTY OF







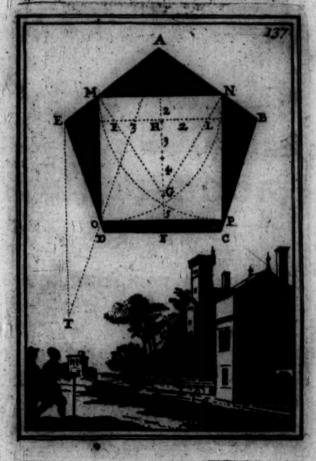
PROPOSITION XV.

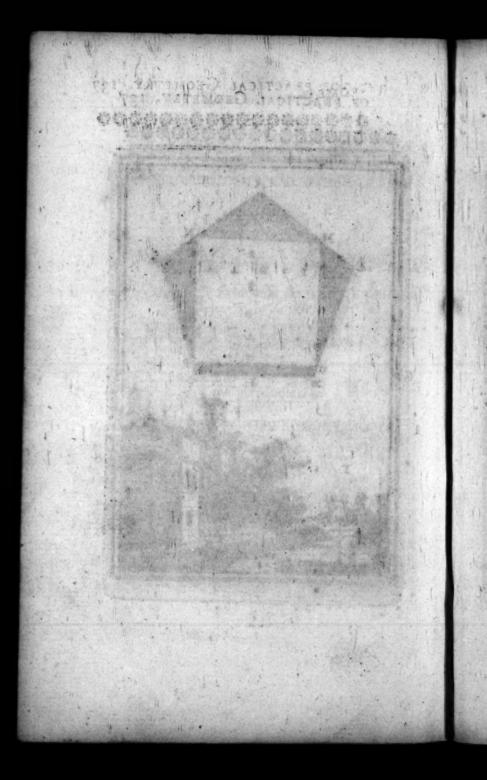
To inscribe a square in a pentagon.

Let ABCDE be the pentagon in which a fquare is to be inferibed.

	Raw the line	BE
Page 54.	let fall the perpendicular	ET
	from the extremity of	BE
	Make this perpendicular	ET
	equal to the line	BE
	Draw the line	AT
	thro' the fection	0
Page 56.	Draw the line	OP
	parallel to the fide	CD
	On the extremities	OAP
Page 50.	Erect the perpendiculars . OA	A. PN
	Draw the line	NM
	The square requir'd will be N	MOP

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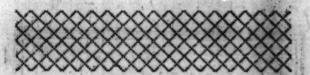
PROPOSOS HIT ON

FOURTH BOOK,

Let A B C be that H T A O which the circlet A B C be to A Stape B become what a size

sic is to be silicumferibed Circumscription of Figures.

Estibation the circumsterence. thro' the raice points indevil A. P. C.



BOOK the FOURTH.

PROPOSITION I.

To circumscribe a circle about a given triangle.

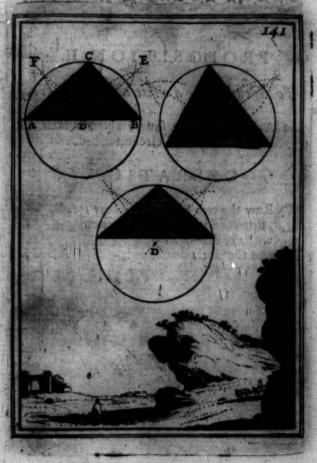
Let ABC be the triangle about which the circle is to be circumscribed.

OPERATION.

Peg. 98. DEscribe the circumference ABC thro' the three points A, B, C and the thing required will be done.









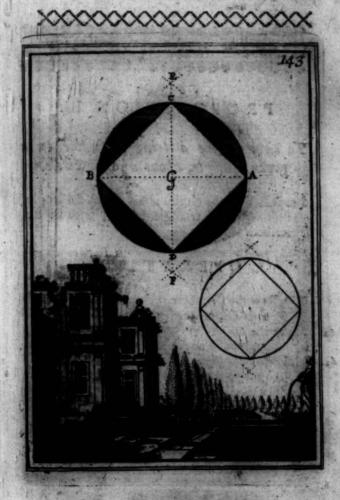
PROPOSITION II.

To circumscribe a circle about a square.

Let ABCD be the fquare about which the circle is to be circumferibed.

Raw the two diagonals	AB,	CD
DRaw the two diagonals upon the interfection or	center *	G
with the distance		G A
Describe the circle demanded	AB	CD





PROPOSITION III.

To circumscribe a triangle similar to a given triangle, about a given circle.

Let DEV be the circle, about which a triangle, fimilar to the triangle FGH, is to be defcribed.

	Raw the diameter	AB
	thro' the center	C
Page 62.	Make the angle	ACE
	equal to the angle	. н
Page 62.	Make the angle	BCD
	equal to the angle	G
	Produce the lines	EC, DC
	towards	R&S
Page 56.	Draw the tangent	NO
	parallel to the line	DR
Page 56.	Draw the tangent	OI
	parallel to the line	ES
Page 56.	Draw also the tangent	NI
	parallel to the diameter	AB
	IN O will be the triangle requir'd	
	triangle FGH, and circumscri	bed about the
	circle D E V.	





PROPOSITION IV.

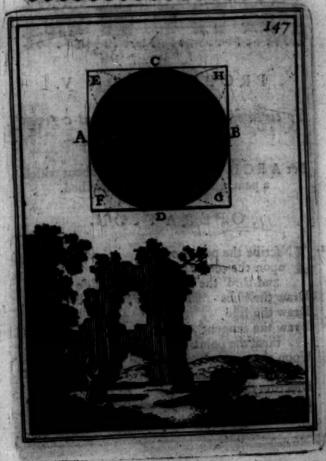
To circumscribe a square about a circle.

Let A B C D be the circle about which a square is to be circumfcribed.

OPERATION.

AB, CD Raw the diameters intersecting each other at right angles in O A. C. B. D upon the points with the distance Describe the semicircles HOG, HOE BOF. FOG Draw the right lines EF, FG, GH, HE thro' the interfections E. F. G. H The fquare demanded will be





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PROPOSITION V.

To circumscribe a pentagon about a given circle.

Let A B C D E be the given circle about which a pentagon is to be circumscribed.

Page 411.	T Nicribe the pentagon	ABCDE
	upon the center	F
	and thro' the middle of ear	ch side
	Draw the lines FO, FP, I	Q, FR, FS
	Draw the line	FA
Page 68.	Draw the tangent	PQ
	thro' the point	A
	Upon the centre	F
	with the radius	FP
	Describe the circle	OPQRS
	Draw the fides of the penta	con demanded
	thro' the fections	O, P, Q, R, S





PROPOSITION VI.

To circumscribe a regular polygon about another of the same sort.

Let B C D E F G be the polygon given, about which another fimilar polygon is to be circumscribed.

PRoduce two fide	s as	BG, EF
Draw the line	t in	H
Draw the line		EI
bisecting the ar		GFH
with the diffance	ce	AI
Draw the radius's	AL, AM,	AN, AO
Draw the fides of the	e of each fide.	
ed, thro' the fe	ctions I, L, M	N. O. P



and a second and a second as a







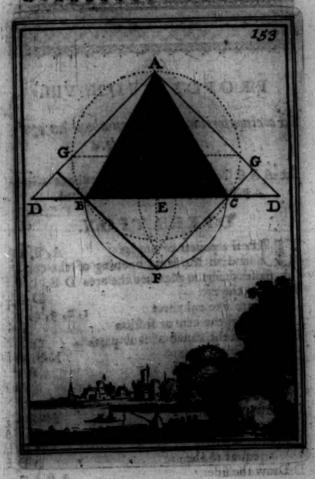
PROPOSITION VII.

To circumscribe a square about a given equilateral triangle.

Let A B C be the equilateral triangle, about which a fquare is to be circumscribed.

OPERATION.

Page 58. T) Ifect the base in the point Produce the base BC both ways towards D&D Make the lines ED&ED equal to the line Upon the point with the distance Describe the semicircle draw the line From the point draw the lines FCG&FBG and the square requir'd will be AGFG



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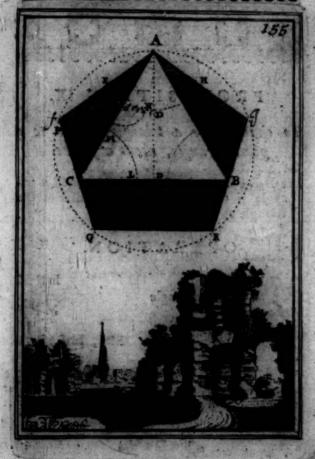


PROPOSITION VIII.

To circumscribe a pentagon about an equilateral triangle.

Let A B C be the triangle given, about which a pentagon is to be circumteribed.

U Pon the points or angles and with the same opening passes describe at pleasure the are	cs DE, LP
Divide the arc into five equal parts	I, 2, 3, 4, 5
And with the distance of four part	s ON
describe the arc Draw the night line	NME AEF
Cut off the arc	MP
Draw the right line	FRCg
Make the arc	PĤ
Draw the fides	AI, IR
The fide	Af, fG IR
will compleat the pentagon d	emanded.





PROPOSITION IX.

To circumscribe a triangle similar to a given triangle, about a square.

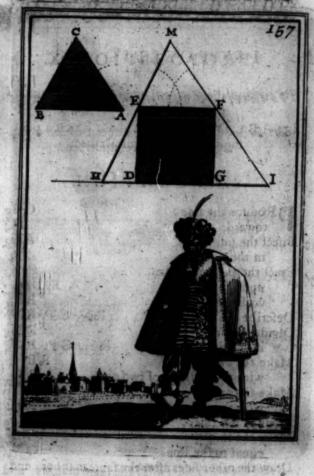
Let DEFG be the fquare about which a triangle is to be circumscribed similar to the triangle A B C.

OPERATION.

Ake the angle EFM Page 62. equal to the angle Page 62. Make the angle MEF equal to the angle Produce the lines ME, MF, DG towards HI I M will be the triangle requir'd, similar to the triangle and circumfcrib'd about the square DEFG

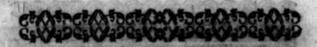


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PROPOSITION X.

To circumscribe a pentagon about a square.

Let A B C D be the fquare about which a pentagon is to be circumscribed.

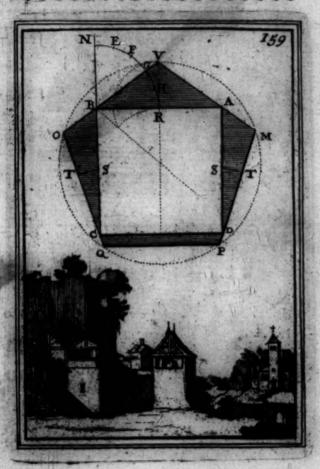
OPERATION.

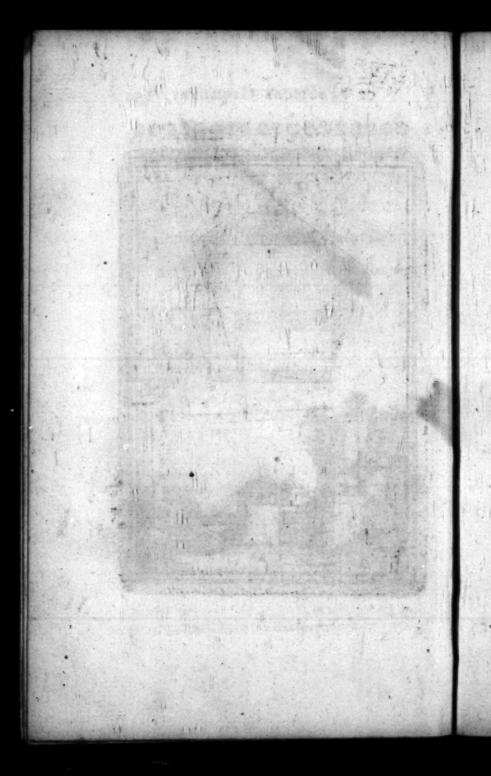
T Roduce the fide	CB
l towards	N
Bifect the fide	AB
in the point	R
Erect the perpendicular	RV
upon the points	B, D, C
with the distance	BR
Describe the arcs	RN, ST, ST
Divide the arc	RN
into five equal parts	RH, GF, EN
Make the angle	RBV
with the distance of two	ENERGICA SE SUSTINICIONES DE COMPANS DE LA COMPANS DE LA COMPANS DE COMPANS D
Make the angles	SCT, SDT
with the distance of one	
Produce the lines	VB, CT to O
Make the line	00
equal to the line	
Draw the other fides after the	
you will have the thing	requir a.

Page 58.

Page 56.

of practical Geometry. 159



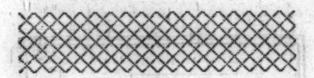


THE

FIFTH BOOK,

OF

Proportional LINES.



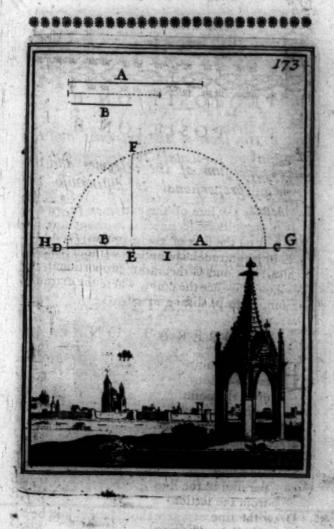
BOOK the FIFTH.

PROPOSITION I.

To find a mean proportional between two given lines.

Let A & B be the two lines between which a mean proportional is to be found.

	Raw an indetermin'd line	GH
	Make	CE
	equal to the line	A
	Make	ED
	equal to the line	В
Pag. 58.	Bifect 1	CD
	in the point	1
	upon the point	1
	and with the diftance	IC
	Describe the semicircle	CFD
	Erect the perpendicular	EF
	This line	EF
	shall be a mean proportional bet	ween A & B



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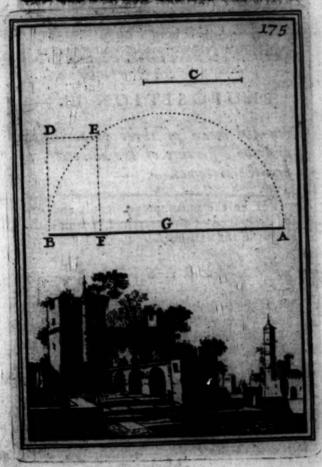


PROPOSITION II.

Given the sum of the extremes and the mean proportional to distinguish the means.

Let A B be the sum of the extremes (i. e. the two magnitudes connected without any diffinction) and C the mean proportional, by whose affishance the point, where the extremes join, is to be distinguished.

Page 68.	Difect the line	AB
	in the point	G
	upon the point	G
	with the interval	GA
	Describe the semicircle	AEB
1.0	Erect the perpendicular	.BD
	equal to the mean proportions	
Page 56.	Draw the line	DE
	parallel to the line	AB
D	from the fection	E
rage 50.	Draw the line	EF
	parallel to the line	BD
	Then will the point where the extrem	nes join be F
	fo that Corits equal	EF
	shall be a mean proportional	
	between	AF & BF
		THE RESERVE WHEN THE RESERVE WAS A STATE OF THE PARTY OF



THE THE BOOK TO



PROPOSITION III.

Given the mean of three proportionals and the difference of the extremes, to find the extremes.

Let G H be the mean proportional, and A B the difference of the extremes, requir'd the length of the extremes.

	Carried Control of Con	1.020mg/dp-101.250
Page 50.	Rect the perpendicular	BC
	at the extremity of the difference	e AB
Page 58.	and equal to the mean	GH
	Bifect the difference	AB
	in the point	D
	Produce both ways towards	E&F
	upon the point	D
	with the distance	DC
	Describe the semicircle	ECF
	The extremes requir'd will be	BE. BF



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H will be the mosa propositional detects the femaliades.

H I and the office line propedly.

B E

PROPOSITION IV.

To cut off from a given line, a part that shall be a mean proportional between what remains and another given right line.

Let A A be the line, of which a part is to be cut off, that shall be a mean proportional between what remains and the line proposed B B

OPERATION.

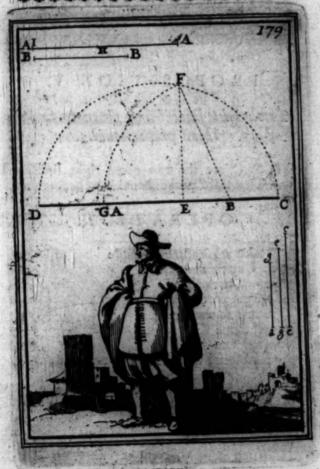
Raw the indefinite line	CD
cut off the lines	DE, EC
equal to the lines	AA&BB
Describe the semicircle	CFD
ge 46. Erect the perpendicular	EF
ge 58. Bisect the line	CE
in the point	B
upon the point	В
with the distance	BF
Describe the arc	FG
Cut off the part demanded	AH
equal to the part	EG

A H will be the mean proportional between the remainder

and the other line proposed

B E

OF PRACTICAL GEOMETRY. 179





PROPOSITION V.

Two right lines being given to find a third proportional.

A B, A C are the two given right lines, to which a third proportional is to be found.

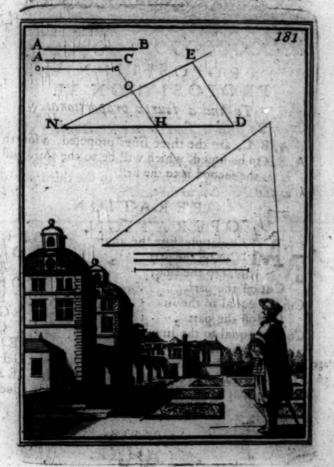
OPERATION.

Aké at pleafure the angle	DNE
Ake at pleasure the angle	NH
equal to the line	AB
Cut off the part	NO
equal to the line	AC
Draw the line to the mis	но
Page 56. Draw the line	DE
parallel to the line	HO

E O will be the third proportional requir'd. all of the chird proper



(considerational considerations)





PROPOSITION VI.

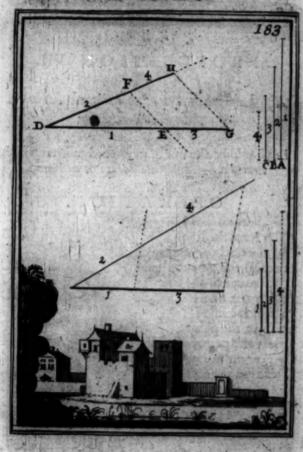
To find a fourth proportional.

A, B, C, are the three lines proposed, a fourth is to be found, which will be to the third just as the second is to the first.

	MAke at pleasure the angle Cut off the part	GDH DE
	equal to the line	A
	Cut off the part	DF
	Cut off the part	EG
	equal to the line	CLINIC DEBUTE OF THE PARTY OF T
10000	Draw the line	EF
Page 56.	Draw the line	GH
	parallel to the line	EF
	FH will be the fourth proportional	demanded.



※*※*※*※*※*※*※*※*※*※





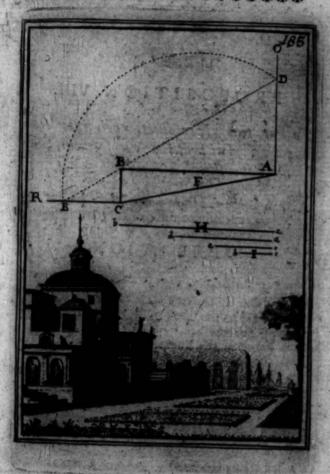


PROPOSITION VII.

To find two mean proportionals between two given lines.

Let I & H be the lines proposed, between which two mean proportionals are to be found.

	Raw the line	AB
	equal to the line	H
	Let fall the perpendicular	BC
	equal to the line	I
	Draw the line	AC
Page 58.	Bisect the line	AC
	in the point	F
Page 50.	Erect the perpendiculars	AO, CR
	upon the point or center	F
	Describe the arc	DE
	fo that the chord	DE
	may touch the angle	B
	AD, CE will be the mean pr	oportionals be-
	tween the given lines	Hal



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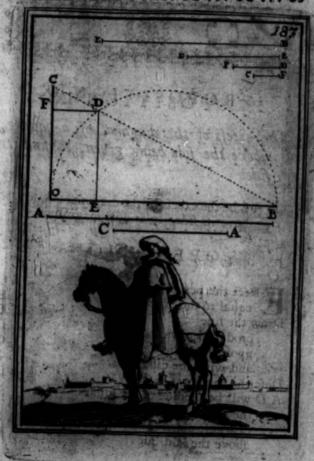


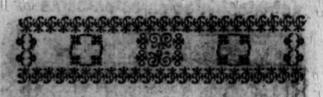
PROPOSITION VIII.

To cut two given lines, each into two parts, so as that the four segments may be proportional, has being given, to am

AB, AC are the lines proposed to be cut acct cording to the propolitiongond of a la

Ake the right angle	BOC
Qut off the line pen	dicaler BO
equal to the linese ex	ses AB
Cut off the line line	00
equal to the lines was	ds AC
Draw the hypothenusoint	BC
Describe the semicircle di	Hance BDO
from the fection	D
Page 56. Draw chelling be the fice	of the fourte DE
parallel to the line	CO
Page 56. and the linesfeeding on	al DF
parallel to the lined f	ide EO
A B will be cut in	E
O C also in	F
fo that BE will be to	D
as E D to	DF, & ED
to DF, as DF is to	FC





PROPOSITION IX

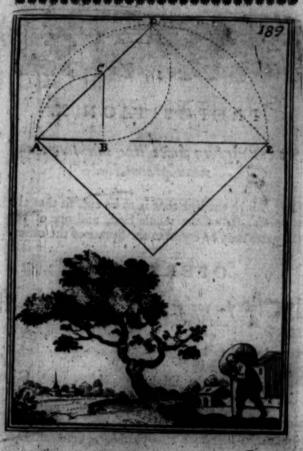
The excess of the diagonal of a square, above the side being given, to find its side.

Let A B be the excess of the diagonal of a square above its side, to find its magnitude.

Page 50.	E Rect the perpendicular BC AB	
	Draw the line	
	produced towards D	
	Describe the are toward BD	Contract of the
	A D will be the fide of the fquare	
	the process and delana AB	
	A above the faid fide the feures AD	



OF PRACTICAL GEOMETRY. 189





PROPOSITION X.

To cut a given finite line in extreme and mean proportion.

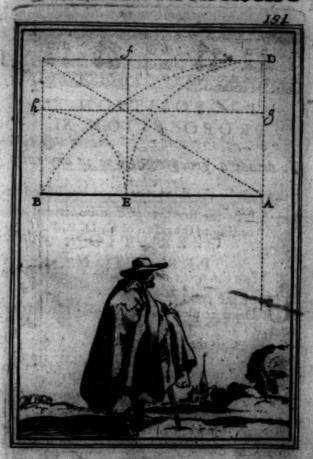
Let A B be the line that is to be cut, fo that the rectangle of the whole line, and one of the parts may be equal to the square of the other.

OPERATION.

		图 和人们。
Page 50.	E Rect the perpendicular Produce it towards	AD
	Produce it towards	
1 8 8	Make	AC
		AB
	equal to half	
2 346	Upon the point	C
	and with the diftance	CB
	Describe the arc	BD
	upon the point	A
	with the diffance	AD
		DE
	Describe the arc	NAME OF THE OWNERS OF THE OWNER,
	The line	AB
	will be cut in the point	. E
	in the proportion requir'd: for i	f vou make
	the rectangle A h of the whol	A B and
	DE Tectangle An of the whol	the fanare
	part B E, it will be equal to	the iduare
	A f made upon the other part	AL

OF PRACTICAL GEOMETRY. 191

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PROPOSITION XI.

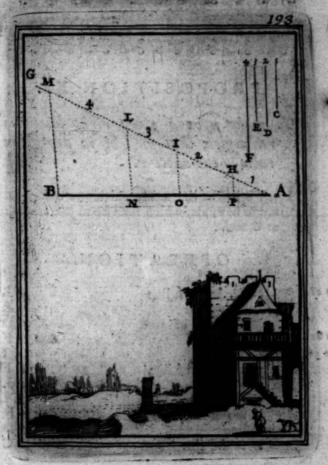
To divide a given right line in any ratio proposed.

Let A B be the line proposed to be divided according to the ratios of C, D, E, F.

OPERATION.

UPon the point or extremity Draw at pleasure the line	A
Draw at pleafure the line	AG
Make	AH
equal to the line or ratio	C
Make	HI
equal to the line	D
Make	1L
equal to the line	E
Make	I, M
equal to the line	F
Draw the line	BM
Draw the lines LN,	IO, HP
parallel to the line	BM
The line A B will be divided in t	he points
	P, O, N
according to the ratio demanded	

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or tractican following

PROPOSITION XII.

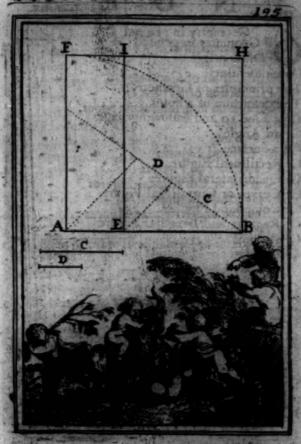
To make upon a given right line two restangles, that shall be in any given ratio to one another.

Let A B be the line upon which two rectangles are to be made, which shall be to one another as C to D.

OPERATION.

Page 184.	Divide the right line at the point	AB
	in the ratio of	C to D
Page 81.	Make the fquare	ABHF
Page 56.	Draw the line	EI
	parallel to the line	AF
	BEIH, AEIF will be the rectangles	requir'd.
	the rectangle	AI
	is to the rectangle	EH
	As the line	D
	is to the line	C

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